DYNAMIC AND MATHEMATICAL MODELS OF THE HYDROIMPULSIVE VIBRO-CUTTING DEVICE WITH A PRESSURE PULSE GENERATOR BUILT INTO THE RING SPRING

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Abstract. Structural calculation scheme of the hydropulse device for vibration cutting with built-in ring with pressure pulse generator (PPG) is considered. On the basis of the structural scheme and cyclogram of the working cycle of the device, its dynamic and mathematical models were developed, in which the hydraulic link is represented by a visco-elastic model of the working fluid (energy carrier) composed of the inertial elastic and dissipative elements (Kelvin-Foya body).

Keywords: mathematical model, dynamic model, hydropulse device, ring spring, frequency, amplitude

MODELE DYNAMICZNE I MATEMATYCZNE HYDRAULICZNEGO URZĄDZENIA IMPULSOWEGO DO CIĘCIA WIBRAJCZYNEGO Z GENERATOREM IMPULSÓW WBUĐOWANYM W SPRĘŻYNĘ PIERŚCIEŃIOWĄ

Streszczenie. Rozważa się schemat konstrukcyjny i projektowy hydraulicznego urządzenia impulsowego do cięcia wibracyjnego z wbudowanym generatorem impulsów ciśnieniowych ze sprężyną pierścieniową (PPG). Na podstawie schematu strukturalnego i cyklu pracy urządzenia opracowano jego modele dynamiczne i matematyczne, w których ogniwo hydrauliczne reprezentowane jest przez lepkosprężysty model cieczy roboczej (nośnika energii), złożony z bezwładnych elementów sprzężystych i dysypacyjnych (cias Kelvin-Foya).

Słowa kluczowe: model matematyczny, model dynamiczny, hydrauliczne urządzenie impulsowe, sprężyna pierścieniowa, częstotliwość, amplituda

Introduction

Vibration cutting and vibration turning in particular, in comparison with conventional turning, have a number of known technological advantages, especially when processing viscous materials such as stainless steels and titanium alloys [6]. The massive introduction of vibration cutting processes is constrained by the practical absence of complete, with a wide range of vibration loading parameters, devices. The authors of the work proposed a number of designs for devices for vibration cutting on the basis of a hydropulse drive using elastic elements of high rigidity such as slit, plate and ring springs [16]. The novelty of the developed designs is confirmed by dozens of patents for utility models of Ukraine.

The purpose of conducting theoretical studies of dynamic processes, which reflect their course in the studied devices, as well as their experimental verification, which establishes the adequacy of the mathematical model to real physical processes, is the development of a scientifically based methodology for the design calculation of the created structure, which allows optimization of its design parameters [5, 6, 7].

1. Analysis of research methods

Research of oscillating systems by theoretical methods [5, 7, 9] is in most cases carried out by researching mathematical models, in particular hydraulic impulse machines – by researching the mathematical model of the executive links in the form of differential equations of motion and equations of the consumption of the energy carrier flowing through the pressure pulse generator (PPG) during the working cycle. In the case of applying the macromodeling method to simplify the original mathematical model, only those variables that influence, in the researcher's opinion, the most, are taken into account in the initial space of variables. Other accounted for effects can be taken into account in a parametric form by changing the coefficients near the considered variables for the case of multiplicative effects or by introducing free terms in the equations for the case of additive effects. This approach is quite often used to simplify the mathematical models of the hydraulic impulse drive, in particular the PPG operation is considered to be instantaneous ("relay"). With this approach, it is not possible to adequately describe the dynamics of this issue, and it creates significant discrepancies between the results of theoretical and experimental research.

In our opinion, studies of simplified models that describe the cycle of the hydraulic impulse vibration drive as a single-act process [2, 10] significantly reduce the correctness of the results of theoretical studies of the processes taking place in the vibration drive and the machine as a whole.

Modern software tools for mathematical modeling of physical processes make it possible to study the dynamics of processes occurring in oscillating systems without simplifying mathematical models. Taking into account all stages of the work cycle of the drive elements ensures the possibility of creating correct methods for the design calculation of the design of the machine or device.

The mathematical models of the hydropulse drive, built on the basis of a detailed step-by-step analysis of the driving cycle of the drive [9, 12], are more correct, and the engineering calculation methods developed on the basis of these models allow to determine the design, power and power parameters of the PPG and the drive, which more precisely with the experimentally established ones under the same conditions initially set during simulation [11, 15].

An important aspect of mathematical models and methods of calculating the hydropulse drives is the choice of model of energy. Known mathematical models of the drive are based in the simplest forms on the "rigid" [10, 13] model of the energy carrier, which does not take into account the elastic and viscous characteristics of the energy carrier, and in more precise forms an "elastic" energy carrier model is used that takes into account the elastic properties of the fluid [3, 8, 14].

2. Theoretical studies

The structural scheme of the hydropulse device for vibration cutting with a built-in ring spring (further RS1) by a pulse pressure generator in a constructive form is shown in Fig. 1.

The device consists of two hydraulically connected units – the PPG and the hydraulic cylinder of the drive in a vibratory movement, for example a turning cutter for radial vibration. The PPG contains a locking element in the form of a valve-spool of 1 mass \( m_s \), the right-hand side (according to the drawing) which is a supporting ring of a ring-spring PPG (RS1) with

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rigidity $k_1$ and mass $m_1$, consisting of a set of outer 2 and inner 3 rings that interact with each other by the mediation of internal and external conical surfaces. The pre-deformation $y_{01}$ of the PPG ring spring is controlled by means of a screw 4 that moves the pressure plunger 5, the left end (which is illustrated) is designed as the second bearing ring RS1. The plunger 5 is sealed with a rubber ring of 6 round sections. The body of the PPG and the device in general is not conventionally shown in Fig. 1.

With the block of the hydraulic cylinder actuator (located in the unit body, like the PPG), the PPG is combined through a common pressure cavity $A$ (hole diameter $d_1$). The hydraulic cylinder consists of a plunger of 7 with a mass $m_2$ compacted by a rubber ring 8. On the right (in the drawing) of the end of the plunger 7, a protrusion is formed which is the support and guide surface of the bearing ring 9 of the ring spring, the hydraulic cylinder (RS2), the stiffness $k_2$ and the mass $m_2$.

RS2 consists of external 10 and internal 11 rings and two identical in shape and sizes of support rings 9 and 12. The rings RS2 are in contact with each other through the inner and outer conical surfaces. The pre-deformation $y_{02}$ of the RS2 is controlled by means of a collar nut 13 that is screwed onto the threaded projection 14 of the device casing conventionally shown by an icon $\times^x$. The nut 13 clicks on the step cap of the RS2 (as shown in the drawing) bearing ring 12 RS2. The nut 13 is locked with a spline nut 16.

In the rectangular aperture of the step cap 13, a cutter 17 is provided, equipped with a cylindrical rod 18 with a buccal ledge. The right part of the rod 18 (behind the buckling protrusion) enters the landing gear in the central hole of the plunger 7, and a spring 19 is installed on the left part of the rod 18 (in front of the hill), with one end resisting the bust of the rod, and the other to the cover 13. The spring 19 is installed during the assembly of the hydraulic cylinder with the estimated pre-deformation and carries the axial pre-fixing of the cutter 17.

In order to provide a stable mode of landing the valve-spool 1 at the end of its reverse, a throttle 20 is provided. The function of the throttle 20 can be provided by the gap in the conjugation of the valve-spool 1 by the diameter $d_1$ of the mortar in the body (or the sleeve in the real construction) of the device or by the experimentally selected folding length $l_1 \geq h_y$ (here $h_y$ – a positive overlap of the spool valve part-spool 1) connects intermediate B and drain C device cavity. The placement cavity RS1 is connected to the drainage cavity with radial openings $a^0$, which are guided in the holes of the device body, are tied to the surface of the outer rings 2 and 10, which RS1 and RS2 during their working deformation, the cylindrical surfaces of the outer rings 2 and 10, which RS1 and RS2 are guided in the holes of the device body, are tied to the surfaces of the holes of the hill under running landings not exceeding 9-10 qualifications. Since, in abso-lute value, the radial deformations of the rings are small, the gaps that provide the named qualities are guaranteed to exclude the possible stitching of the rings [1, 4, 17].

The "opening" pressure of the PPG is determined by the known dependence [3, 14, 16]

$$p_i \geq k_1 \cdot y_{01}/A_4 = 4k_1 \cdot y_{01}/(\pi d_1^2) = 0.785k_1 \cdot y_{01}/d_1^2,$$

(1)

where $A_4 = \pi d_1^2/4 = 0.785d_1^2$ – the area of the cross-section along the facet of the valve-spool 1 for its small diameter $d_1$ (the first degree of sealing of the sealing element of the PPG – valve-spool 1), provided that the sealing is carried out on a facet of small width, which can be calculated according to the formulas given in the work [17].

The movement of the plunger 7 of the hydraulic cylinder of the drive of the cutter 17 in the vibrational movement will begin after the increase in the pressure of the energy carrier in the pressure cavity $A$ to the level (without taking into account frictional forces between the plunger 7 and its guiding surface)

$$p_i \geq k_2 \cdot y_{02}/A_5 = 4k_2 \cdot y_{02}/(\pi d_2^2) = 0.785k_2 \cdot y_{02}/d_2^2,$$

(2)

where $p_i$ – stationary pressure of the energy carrier, at which the plunger 7 movement begins 7; $A_5 = \pi d_2^2/4 = 0.785d_2^2$ – square cross-section of the plunger 7.

The maximum possible displacement of the plunger 7 and the cutter 17, because due to the force of the spring 19, it is located with a plunger 7 in a rigid contact, can be estimated from the equation of dynamic equilibrium:

The maximum possible displacement $h_{y,\max}$ of the plunger 7 and the cutter 17, because due to the force of the spring 19, it is located with a plunger 7 in a rigid contact, can be estimated from the equation of dynamic equilibrium:

$$p_i \cdot A_5 \geq k_2 (y_{02} + h_{y,\max})$$

(3)

where

$$h_{y,\max} = p_i \cdot A_5 / k_2 - y_{02,\max} \approx 0.785p_i d_2^3 k_2^{-1}.$$

(4)

The displacement $h_f$ of the plunger 7 is essentially the amplitude of the vibration oscillations of the cutter 17 and, as can be seen from dependence (4), can be regulated by changing the energy pressure $p_i$ and previous deformation $y_{02}$ of the RS2.

Fig. 1. Structural diagram of the hydropulse device for vibratory turning device with a pressure pulse generator built into the ring spring PPG
3. Results

Taking into account the given structure of assumptions and the oriented cyclogram of the working cycle [11, 12, 15], the dynamical models of the direct (Fig. 2a) and reverse (Fig. 2b) moves of the valve-spool 1 and plunger 7 (cutter 17) (see Fig. 1) they consist of two lumped masses \( m_1 \) and \( m_2 \) interact with \( H_L \), in the form of connected parallel elastic \( k_e \) and dissipative \( c_e \) elements, due to the transfer ratios \( U_{0102} \) and \( U_{00} \cdot H_L \) during the operating cycle of the device deforms with variable speed \( \dot{x}_m \) in directions \( x_m \).

Moving masses \( m_1 \) and \( m_2 \) during their direct (\( y_{11} \) and \( y_{12} \)) and reverse (\( y_{21} \) and \( y_{22} \)) moves counteract the positional forces of elastic resistance, which are characterized by stiffness \( k_e \), \( k_2 \) and \( k_3 \) viscous resistance, the level of which is determined by the coefficients \( c_1 \) and \( c_2 \) and velocities \( \dot{y}_{1e}, \dot{y}_{2e}, \dot{y}_{12}, \dot{y}_{22} \) by the force of dry friction \( R \) and the force of cutting \( F_c \), which supposed to act only during direct mass \( m_2 \) movement.

An important point in the use of RS1 and RS2 as power elastic elements of the PPG and the hydraulic cylinder of the drive cutter 17 in the vibratory motion is to determine their rigidity and deformation (deposition) under the action of the maximum axial forces acting on RS1 \( F_{1\text{max}} \) and RS2 \( F_{2\text{max}} \).

\[
F_{1\text{max}} = p_{\text{max}} \cdot A_1; \quad F_{2\text{max}} = p_{\text{max}} \cdot A_2; \quad (5)
\]

where \( p_{\text{max}} \) – the maximum possible pressure „opening” the PPG.

Fig. 2. Dynamic models of direct a) and reverse b) mass movements \( m_1 \) and \( m_2 \)

The determination of the rigid and structural parameters of RS1 and RS2 can be made on the basis of known works [4, 17] in the calculation and design of ring springs.

To construct a mathematical model of the device for vibration cutting, the initial dynamic models of direct and reverse moves of the model of direct and reverse mass movements \( m_1 \) and \( m_2 \) expeditiously to simplify the principle of dismemberment [15] by bringing the \( H_L \) to mass \( m_1 \) and \( m_2 \).

As a result of this reduction, we obtain four simple dynamic models of direct (Fig. 3a, b) and reverse (Fig. 3c, d) of mass \( m_1 \) and \( m_2 \).

On the basis of the principle of D'Alembert, we compile with the help of the given dynamic models the differential equations of the movement of the valve-spool 1 (mass \( m_1 \)) and the executive link of the device of the plunger 7 (cutter 17) (mass \( m_2 \), see Fig. 1) during the moves:

1. When \( x_{10} \geq x_{02} \geq x_{03} \):

\[
\begin{align*}
 m_1 \ddot{y}_{1,2} &= U_{0102} \cdot k_e \left[ \dot{y}_{11} - \dot{y}_{12} - k_e \left( y_{11} - y_{12} - U_{0102} \right) - c_e \left( \dot{y}_{11} - \dot{y}_{12} \right) \right], \\
 m_2 \ddot{y}_{1,2} &= U_{00} \cdot k_e \left[ \dot{y}_{21} - \dot{y}_{22} - k_e \left( y_{21} - y_{22} - U_{00} \right) - c_e \left( \dot{y}_{21} - \dot{y}_{22} \right) \right], \quad (7)
\end{align*}
\]

2. When \( x_{02} \geq x_{03} \geq 0 \):

\[
\begin{align*}
 m_1 \ddot{y}_{1,2} &= k_e \left( y_{11} + h_1 y_{12} - y_{12} \right) - U_{0102} - k_e \left[ \dot{y}_{11} + \left( 0 - h_1 \right) - \dot{y}_{12} \right] - U_{0102} - c_e \left( y_{11} - y_{12} \right) - c_e \dot{y}_{12}, \quad (8)
\end{align*}
\]

3. When \( y_{12} \leq y_{11} \leq h_1 \), \( x_{4122} = x_{412} \cdot U_{0102} \), \( \ddot{x}_{4122} = \ddot{x}_{412} \cdot U_{0102} \); \( x_{4122} \) and \( \ddot{x}_{4122} \) are determined by changes \( U_{0102} \) on the interval \( 0 \leq y_{12} \leq h_1 \).

4. When \( y_{11} \leq y_{12} \leq h_1 \), \( x_{4120} = x_{412} \cdot U_{00} \), \( \ddot{x}_{4120} = \ddot{x}_{412} \cdot U_{00} \); \( x_{4120} \) and \( \ddot{x}_{4120} \) are determined by changes \( U_{00} \) on the interval \( 0 \leq y_{11} \leq h_1 \).

5. When \( y_{12} \leq y_{11} \leq h_1 \), \( x_{4123} = x_{412} \cdot U_{03} \), \( \ddot{x}_{4123} = \ddot{x}_{412} \cdot U_{03} \); \( y_{1f}, y_{12f}, y_{12}, \dot{y}_{1f}, \dot{y}_{12f}, \ddot{y}_{12f} \) – respectively, the current coordinates and velocities of the masses \( m_1 \) and \( m_2 \) during the direct and the return of their moves; \( y_{03} \) – predeformation of the spring 19 (see Fig. 1).

Fig. 3. Simplified dynamic models of direct (a, b) and inverse (c, d) mass movements \( m_1 \) and \( m_2 \)
Differential equations of systems (7) and (8), in order to exclude free members, replace variables \( y_{x1}, y_{x2}, y_{x3} \) and \( y_{z2} \) variables:

\[
\begin{align*}
\dot{z}_{x1} &= y_{x1} + \alpha_{m1} U_{0}(t) + \alpha_{m2} U_{0}(t), \\
\dot{z}_{x2} &= y_{x2} + \alpha_{m3} U_{0}(t) + \alpha_{m4} U_{0}(t), \\
\dot{z}_{x3} &= \alpha_{m5} U_{0}(t) + \alpha_{m6} U_{0}(t), \\
\dot{z}_{z2} &= \alpha_{m7} U_{0}(t),
\end{align*}
\]

\[
\begin{align*}
\dot{y}_{x1} &= u_{x1} + \alpha_{y1} U_{0}(t), \\
\dot{y}_{x2} &= u_{x2} + \alpha_{y2} U_{0}(t), \\
\dot{y}_{x3} &= \alpha_{y3} U_{0}(t), \\
\dot{y}_{z2} &= \alpha_{y4} U_{0}(t),
\end{align*}
\]

\[
\begin{align*}
\dot{z}_{z2} &= \alpha_{m8} U_{0}(t),
\end{align*}
\]

where:

\[
\begin{align*}
\omega_{k2} &= \sqrt{k_{k2} m_{k2}}, \\
\omega_{p1} &= \sqrt{\omega_{k1} m_{k1}}, \\
\omega_{p2} &= \sqrt{\omega_{k2} m_{k2}}, \\
\omega_{y1} &= \sqrt{\omega_{y1} m_{y1}}, \\
\omega_{y2} &= \sqrt{\omega_{y2} m_{y2}}, \\
\omega_{y3} &= \sqrt{\omega_{y3} m_{y3}}, \\
\alpha_{m1} &= \gamma_{1} \omega_{y1} m_{y1}, \\
\alpha_{m2} &= \gamma_{2} \omega_{y2} m_{y2}, \\
\alpha_{m3} &= \gamma_{3} \omega_{y3} m_{y3} - \omega_{p1} \omega_{p2} \omega_{k2} m_{k2},
\end{align*}
\]

Differential equations of devices with a hydropulse drive. For a hydraulic drive invariant to the system of the device links, will allow to create scientifically grounded method of design calculation of similar designs of devices with a hydropulse drive.

References

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